LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600 034

B.Sc. DEGREE EXAMINATION – STATISTICS

FIRST SEMESTER - APRIL 2010

ST 1503 - PROBABILITY AND RANDOM VARIABLES

Date & Time: 30/04/2010 / 9:00 - 12:00 Dept. No.

Max.: 100 Marks

SECTION – A $(10 \times 2 = 20 \text{ Marks})$

Answer ALL the questions

- 1. Define Probability of an event.
- 2. For two independent events A and B , P(A)=0.4 , P(B)=0.5, find $P(A\cup B)$.
- A problem in Statistics is given to three students whose chances of solving it are 1/3. 1 /4, 1/5 respectively. Find the chance that the problem will be solved.
- 4. There are 20 silk sarees and 50 cotton sarees in a shop. In how many ways a lady can choose one cotton saree and one silk saree?
- 5. Two coins are tossed. If E_1 is the event "head on first coin", E_2 the event, "head on second coin" and E_3 the event, "the coins match, both are heads or both tails. Show that the three pair wise independent events are not independent.
- 6. Let A and B be two events such that P(A) = 0.4, $P(A \cup B) = 0.8$ and P(B) = p. What is choice of p for which A and B are independent?
- 7. A bag contains 3 red and 5 green balls . Two balls are drawn at random without replacement. Find the probability that both balls drawn are green.
- 8. Four coins are tossed simultaneously. What is the probability of getting 2 heads and 2 tails.
- 9. The pdf of a continuous random variate X is given by $f(x) = k x^2 (1-x), 0 < x < 1$

= 0 , elsewhere

Find the constant k.

10. Define mathematical expectation.

SECTION- B ($5 \times 8 = 40 \text{ Marks}$)

Answer any FIVE questions.

- 11. Using the Axioms of probability, prove the following:-
 - (i) If $B \subset A$, then $P((A \cap \overline{B})) = P(A) P(B)$
 - (ii) If $B \subset A$, then $P(B) \leq P(A)$
 - (iii) For any two events A and B, and P ($\overline{A} \cap B$) = p(B) p(A \cap B)

12. From a random number table, a two digit number is selected at random. What is the probability that

- (i) it is divisible by 4
- (ii) it is divisible by 10
- (iii) it is divisible by 10 or by 4

Note: Take 00 divisible by 10 as well as 4.

- 13. A, B and C go for bird hunting. A has record of 1 bird out of 2, B gets 2 out of 3 and C gets 3 out of 4. What is the probability that they will kill a bird at which all shoot simultaneously?
- 14. There are two identical boxes containing 4 White and 3 Black balls and 3 White and 7 Black balls. A box is chosen at random and a ball is drawn from it. Find the probability that the ball is Black.
- 15. If two dice are thrown, what is the probability that the sum is (a) greater than 8 and (b) neither 7 nor 11?
- 16. A bag contains 4 Red and 3 Blue balls. Two drawings of 2 balls are made. Find the chance that the first drawing gives 2 Red balls and the second drawing 2 Blue balls.
 - (a) if the balls are returned to the bag after the first draw.
 - (b) if the balls are not returned.
- 17. State and Prove Law of Total probability for 3 events.
- 18. a) Define: Probability mass function and Distribution function.

b)In a continuous distribution whose relative frequency density is given by

f(x) = k x (2-x), $0 \le x \le 2$,

find the value of k.

Answer any TWO questions

19. a) A purse contains 4 nickel coins and 9 copper coins, while another purse contains 6 nickel and 7 copper coins. A purse is chosen at random and a coin is drawn at random from it. What is the probability that it is a nickel coin?

b) If P(A) = 1/4, P(B) = 2/5 and $P(A \cup B) = 1/2$, fins (i) $P(A \cap B)$ and (ii) $P(A \cup B)$, where A, B are mutually exclusive.

- 20 a) An unbiased coin is tossed three times. Let A be the event "not more than one head " and let B be the event " at least one of the each face". Are A and B independent?
 - b) Three urns contain respectively 1 White and 2 Black balls; 3 White and I Black ball; 2 White and 3 Black balls. One ball is taken from each urn. What is the probability that among the balls drawn, there are 2 White and 1 Black?
- 21a) State and prove Baye's Theorem
 - b) There are two identical boxes containing 4 white and 3 red balls, and 3 white and 7 red balls.A box is chosen at random and a ball is drawn from it. Find the probability that the ball is red.
 - c) A class consists of 50 students out of which the number of girl students is 10. In the class 2 girls and 5 boys are rank holders in the previous examination. If a student is selected at random from the class and is found to be a rank holder, what is the probability that the student selected is a girl?
 - 22 a)Two cards are drawn. i) successively with replacement

ii) simultaneously (successively without replacement) from a well shuffled deck of 52 cards. Find the probability distribution of the number of aces.

b) If t is a non-negative real number, show that the function defined by $r = t (1 - t) x^{-1}$

$$f(x) = e^{-t} (1 - e^{-t})^{x}$$

Can represent a probability function of a discrete random variable X assuming the values

1,2,3,....

Find expectation of X.

********** All the Best **********